

Quiz 10

Name: Key

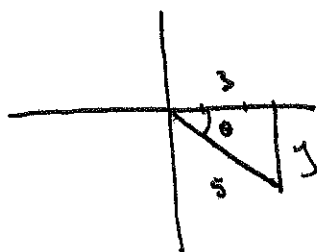
Math 115, Fall 2016

Thursday Discussion Time: _____

Directions: You have 20 minutes to complete this quiz. Read each problem carefully. There are three problems on the back of this page. Please put a box around your answers. No calculators are allowed.

1. (2 points)

If $\cos(\theta) = \frac{3}{5}$ and θ terminates in quadrant IV, determine $\sin(\theta)$.

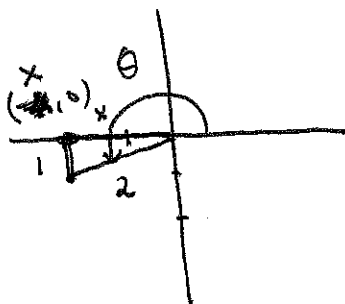


$$3^2 + y^2 = 5^2 \Rightarrow y^2 = 25 - 9 = 16 \Rightarrow y = -4$$

$$\sin(\theta) = -\frac{4}{5}$$

2. (2 points)

If $\sin(\theta) = -\frac{1}{2}$ and $\pi < \theta < \frac{3\pi}{2}$, determine $\cos(\theta)$.



$$x^2 + 1^2 = 2^2 \Rightarrow x^2 = 3 \Rightarrow x = -\sqrt{3}$$

$$\cos \theta = -\frac{\sqrt{3}}{2}$$

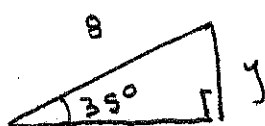
3. (2 points)

Determine the exact value of $\sin\left(\frac{\pi}{6}\right)\cos\left(\frac{\pi}{4}\right)$.

$$\sin\left(\frac{\pi}{6}\right) = \frac{1}{2}, \quad \cos\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2}$$

$$\sin\left(\frac{\pi}{6}\right)\cos\left(\frac{\pi}{4}\right) = \frac{1}{2} \cdot \frac{\sqrt{2}}{2} = \boxed{\frac{\sqrt{2}}{4}}$$

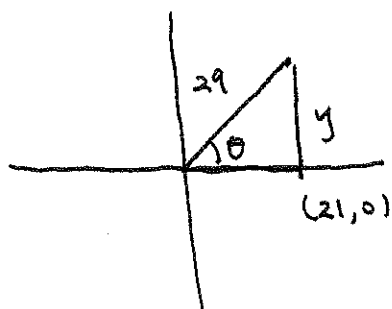
4. (2 points)

If a right triangle has an angle $\theta = 35^\circ$ and the hypotenuse has length 8, determine the length of the side of the triangle that is opposite to θ . Leave your answer in exact form.

$$\sin 35^\circ = \frac{y}{8}$$

$$\boxed{y = 8 \sin(35^\circ)}$$

5. (2 points)

If $\cos(\theta) = \frac{21}{29}$ and θ terminates in quadrant I, determine $\tan(\theta)$.

$$21^2 + y^2 = 29^2 \Rightarrow y^2 = 29^2 - 21^2 = (29+21)(29-21) \\ = (50)(8) = 2^4 \cdot 5^2$$

$$\Rightarrow y = 2^2 \cdot 5 = 20$$

$$\boxed{\tan \theta = \frac{20}{21}}$$