

The ac method

$$ax^2 + bx + c \quad (1)$$

- ① We want to find two numbers whose product is $a \cdot c$ and whose sum is b .
- ② Break down the middle term using the two numbers you found as coefficients.
- ③ Factor by grouping

Ex. Factor the polynomial

$$6x^2 - 11x - 7$$

$$6x^2 + 3x - 14x - 7$$

$$= 3x(2x+1) - 7(2x+1)$$

$$= (2x+1)(3x-7)$$

factored!!

$$a=6 \quad b=-11 \quad c=-7$$

Prod

$a \cdot c$

$$6 \cdot (-7)$$

$$-42$$

$$\begin{array}{r} 3 \overline{) -42} \\ -14 \end{array}$$

Sum

$$-11$$

$$\begin{array}{r} -11 \\ -11 \end{array}$$

ex. Sometimes you are asked to go a step further and solve an equation for x .

(2)

ex. Solve

$$\begin{aligned}x^2 - 13x - 30 &= 0 \\x^2 - 15x + 2x - 30 &= 0 \\x(x-15) + 2(x-15) &= 0 \\(x-15)(x+2) &= 0 \\x-15=0 & \quad x+2=0 \\x=15 & \quad x=-2\end{aligned}$$

① Zero must be on one side
② factor other side

prod	sum
$1 \cdot (-30)$	
-30	-13
$-15 \mid 2$	-13

③ use zero factor property to solve

If $a \cdot b = 0$, then $a = 0$ or $b = 0$

Special products

Difference of two squares

$$a^2 - b^2 = (a-b)(a+b)$$

ex. ^{Factor} $9x^2 - 4 = (3x)^2 - (2)^2$

$$= (3x+2)(3x-2)$$

Perfect Squares

$$a^2 + 2ab + b^2 = (a+b)^2$$

$$a^2 - 2ab + b^2 = (a-b)^2$$

ex.

$$4x^2 + 12x + 9 = (2x)^2 + 2(2x)(3) + (3)^2 = (2x+3)^2$$